## Computer Systems Assignment 1

Answer the questions and submit a PDF to Moodle with your answers. We advise you use the tools covered in the module as far as possible and paste images into a Word document or similar. Then convert to PDF, and upload.

For Boolean expressions you can either write these by hand and add photos, or use Word's mathematical equation input in the Insert menu.

1. Design a simple logic circuit using the following building blocks of logic design.
(a) $(\neg A \wedge B) \vee(A \wedge \neg B \wedge C)$
(b) $\neg(A \wedge(B \vee C)) \wedge B$
(c) $\neg(A \wedge B) \vee \neg(\neg A \vee C)$
2. Write the following logic circuits as Boolean expressions.


3. For the logic circuits in Question 2 define the truth tables.
(a)
(b)
(c)
4. Construct the finite state machines given the state transition tables provided.
(a)
(b)

| (a) | Start State | Input | End State |
| :---: | :---: | :---: | :---: |
|  | - | Initial | $q 0$ |
|  | q0 | 1 | $q 0$ |
|  | q0 | 0 | $q 1$ |
|  | q1 | 1 | q2 |
|  | q1 | 0 | q1 |
|  | q2 | 0 | q2 |
|  | q2 | 1 | q3 |
|  | q3 | 0 | q3 |
|  | q3 | 1 | q3 |
| (b) | Start State | Input | End State |
|  | - | Initial | $q 0$ |
|  | q0 | $b$ | q1 |
|  | $q 0$ | $a$ | $q 0$ |
|  | q0 | c | q4 |
|  | q1 | $b$ | q1 |
|  | q1 | $a$ | q2 |
|  | q1 | c | q0 |
|  | $q 2$ | $b$ | $q 1$ |
|  | q2 | $a$ | q2 |
|  | q2 | c | q3 |
|  | q3 | c | q4 |
|  | q3 | $b$ | q2 |
|  | q3 | $a$ | q3 |
|  | q4 | c | q4 |
|  | q4 | $b$ | q1 |
|  | q4 | $a$ | q3 |


| (a) | Start State | Input | End State |
| :---: | :---: | :---: | :---: |
|  | - | Initial | $q 0$ |
|  | q0 | 1 | $q 0$ |
|  | q0 | 0 | $q 1$ |
|  | q1 | 1 | q2 |
|  | q1 | 0 | q1 |
|  | q2 | 0 | q2 |
|  | q2 | 1 | q3 |
|  | q3 | 0 | q3 |
|  | q3 | 1 | q3 |
| (b) | Start State | Input | End State |
|  | - | Initial | $q 0$ |
|  | q0 | $b$ | q1 |
|  | $q 0$ | $a$ | $q 0$ |
|  | q0 | c | q4 |
|  | q1 | $b$ | q1 |
|  | q1 | $a$ | q2 |
|  | q1 | c | q0 |
|  | $q 2$ | $b$ | $q 1$ |
|  | q2 | $a$ | q2 |
|  | q2 | c | q3 |
|  | q3 | c | q4 |
|  | q3 | $b$ | q2 |
|  | q3 | $a$ | q3 |
|  | q4 | c | q4 |
|  | q4 | $b$ | q1 |
|  | q4 | $a$ | q3 |

5. Provide the state transition table for the following state machines.

(a)

(b)
6. For the two state machines provided in Question 5, determine if the following strings will be accepted by the state machine.
(a) abbaa
(b) $b b a a b a$
(c) $a b b a$
(d) $b a b a$
(e) $b a b b b a b a$
7. Design state machines that will accept the following string definitions.
(a) A string of 0 s and 1 s such that any string with at least 101 is accepted.
(b) A string of 0 s and 1 s such that any string is a multiple of four digits in length, ignoring any leading zeros. For example,

- 1100 is acceptable (length of string is four).
- 0110 is not acceptable (length without leading 0s is three).
- 001000 is acceptable (length of string without leading 0s is four).
- 10000000 is acceptable (length of string is eight, which is a multiple of four).
(c) A string of 0 s and 1 s such that three 1 s appear in a row anywhere in the string.

| Question | Points | Score |
| :---: | :---: | :---: |
| 1 | 12 |  |
| 2 | 11 |  |
| 3 | 7 |  |
| 4 | 6 |  |
| 5 | 6 |  |
| 6 | 10 |  |
| 7 | 8 |  |
| Total: | 60 |  |

